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*On the parity of  $k$ -th powers mod  $p$ .*

Given a prime  $p$ , Lehmer asked for the number  $N_{-1}$  of even residues in  $\mathbb{Z}/p$  whose inverse is odd modulo  $p$ . Zhang proved that  $N_{-1} \sim p/4$ . We consider a more general problem: given  $k, A$  any integers with  $p$  not dividing  $A$ , determine the number  $N_k$  of even residues such that  $Ax^k$  is odd modulo  $p$ . In this more general case,  $N_k$  is not always asymptotic to  $p/4$ . We briefly discuss the use of exponential sum methods to prove many cases where  $N_k \sim p/4$  as well as highlight a few examples where bias occurs. (Received September 22, 2009)