## 1056-15-394 Junsheng Fang, David Larson and Stephen Rowe\* (srowe12@gmail.com), 1190 Main Street, Box 212, Jupiter, FL 33458. On Property P<sub>1</sub> and Spaces of Operators. Preliminary report.

A problem posed by David Larson asks whether every subspace with property  $P_1$  is two-reflxive, or equivalently, is its preannihilator the closed span of rank  $\leq 2$  operators. A space of operators  $S, \subseteq M_n(\mathbb{C})$ , is said to have property  $P_1$  if every element of  $M_n(\mathbb{C})$  can be written as a rank-1 matrix plus an element of the preannihilator of S. The preannihilator,  $S_{\perp}$ , is the set of all operators, f, such that  $Tr(fs) = 0 \quad \forall s \in S$ . We investigate the structure of spaces that have property  $P_1$ . We say an algebra A is a maximal  $P_1$  algebra if there does not exist any algebra containing A that also has property  $P_1$ . We show that semi-simple algebras always have property  $P_1$  and that when  $A \subset M_n(\mathbb{C})$  is a semi-simple algebra with dimension n, then A is a maximal  $P_1$  algebra. (Received September 03, 2009)