

1056-26-104

**Maxim Zinchenko\*** (maxim@caltech.edu). *On the Hilbert Transform of a Measure.*

We give a criterion for pure absolute continuity of a measure in terms of its Hilbert transform. Explicitly, we prove that  $\lim_{t \rightarrow \infty} t|E \cap \{x : |H_\mu(x)| > t\}| = 0$  if and only if  $\mu_s(E) = 0$ , where  $\mu$  is a finite positive measure on  $\mathbb{R}$ ,  $\mu_s$  its singular part,  $H_\mu$  its Hilbert transform, and  $E \subset \mathbb{R}$  is a homogeneous set in the sense of Carleson. The result has applications in the spectral theory of Schrödinger, Jacobi, and CMV operators.

This is joint work with Alexei Poltoratski and Barry Simon. (Received July 27, 2009)