Jeffrey L Stuart* (jeffrey.stuart@plu.edu), Mathematics Department, Pacific Lutheran University, Tacoma, WA 98447. Inverses for Matrices that Don't Have Inverses.
Every student who takes linear algebra learns that the matrix $A$ has an inverse $B$ if and only if $A B=B A=I$, and that if you apply row operations to the augmented matrix $[A \mid I]$ to obtain $[\operatorname{rref}(A) \mid M]$ where $\operatorname{rref}(A)$ denotes the reduced row echelon form of $A$, then $M$ is the inverse of $A$ exactly when $\operatorname{rref}(A)=I$. What happens when $A$ does not have an inverse? This simple question provides a natural opportunity to introduce students to how mathematicians weaken requirements, posit generalizations and seek to preserve desirable properties. Along the way, students learn what $M$ is trying to tell them. (Received September 18, 2009)

