Meeting: 1003, Atlanta, Georgia, AMS CP 1, AMS Contributed Paper Session

1003-11-537 Charles T. Pooh* (pooh@math.uga.edu), Department of Mathematics, University of Georgia, Athens, GA 30602. Explicit Galois stable sets of algebraic integers in a given set of points.

Let E be a compact set in the plane, stable under complex conjugation and having logarithmic capacity $\gamma(E)$. We prove effective versions of the classical theorems of Fekete and Fekete-Szegö. Specifically, we show that if $\gamma(E) < 1$ then there is a monic polynomial $P(w) \in \mathbb{Z}[w]$, whose degree and coefficients are bounded explicitly in terms of $\gamma(E)$, such that the region |P(w)| < 1 contains an ϵ -neighborhood of E. If $\gamma(E) \geq 1$, each ϵ -neighborhood of E contains a level curve |P(w)| = c where the integer c, the degree and the coefficients of the monic polynomial $P(w) \in \mathbb{Z}[w]$ are bounded explicitly in terms of ϵ and $\gamma(E)$. (Received September 21, 2004)