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*Rings of Continuous Functions on Spaces of Finite Rank and the SV Property.*

Let  $C(X)$  denote the ring of continuous real-valued functions defined on the compact space  $X$ . A point  $x \in X$  is said to have rank  $n$  if, in  $C(X)$ , there are  $n$  minimal prime  $\ell$ -ideals contained in the maximal  $\ell$ -ideal  $M_x = \{f \in C(X) : f(x) = 0\}$ . The space  $X$  has finite rank if there is an  $n$  such that every point  $x \in X$  has rank at most  $n$ . We call  $X$  an SV space if  $C(X)/P$  is a valuation domain for each minimal prime ideal  $P$  of  $C(X)$ . Every compact SV space has finite rank and it is unknown if a compact space of finite rank is necessarily SV.

For a bounded continuous function  $h$  defined on a cozeroset  $U$  of  $X$ , we say there is an  $h$ -rift at  $z \in X$  if there is no extension of  $h$  in  $C(U \cup \{z\})$ . I will show that the set of points with  $h$ -rift is a subset of the set of points of rank greater than 1 and that whether or not a compact space of finite rank is SV depends on a characteristic of the closure of the set of points with  $h$ -rift for each  $h$ . If  $X$  has finite rank and the set of points with  $h$ -rift is an F-space for each  $h$ , then  $X$  is an SV space. Also, if every  $x \in X$  has rank at most 2, then  $X$  is an SV space if and only if for each  $h$ , the set of points with  $h$ -rift is an F-space. (Received September 24, 2005)