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A matrix  $A \in M_n(\mathbb{C})$  is called *Hermitian* if  $A = A^*$ . A Hermitian matrix with nonnegative eigenvalues are called *positive semi-definite (PSD)* matrices. Given a Hermitian matrix  $A$  we associate a simple, undirected graph  $G$  with  $V(G) = \{1 \cdots n\}$  and edges  $E(G) = \{(i, j) \mid a_{ij} \neq 0, i \neq j\}$ . The graph is independent of the diagonal entries of  $A$ . The *minimum positive semi-definite (PSD) rank* of  $G$ , denoted  $msr(G)$ , is the minimum rank of  $A$  where  $A$  varies over all PSD matrices with graph  $G$ .

For a simple connected graph  $G$  we define the *tree size* of  $G$ , denoted  $ts(G)$ , as the number of vertices in the maximum induced tree in  $G$ , and the *clique cover number*, denoted  $c(G)$ , as the smallest number of cliques needed to cover all the edges in  $G$ .

In this paper we present some results on the minimum PSD rank of some classes of graphs, including bipartite graphs, non-chordal graphs for which  $msr(G) = c(G)$ , and graphs for which  $msr(G) = ts(G) - 1$ . Also, we present some additive properties of  $msr(G)$  for a graph  $G$  that can be identified as overlapping sum of two subgraphs by considering the effect of edge cancellation on the graph.

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