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Arturo Magidin* (magidin@member.ams.org), Mathematics Department, 217 Maxim Doucet Hall, P.O. Box 41010, Lafayette, LA 70504-1010. *Capability of nilpotent groups of class two and prime exponent*. Preliminary report.

A group G is capable if $G \cong K/Z(K)$ for some group K . Using the nilpotent product, one can translate the problem of whether a given p -group of class two and exponent p is capable to a question of linear algebra. Using this translation, a number of new results have been obtained, such as a new sufficient condition based on the ranks of $G/Z(G)$ and $[G, G]$. Explicitly, let a be a positive integer; writing $a = \binom{T}{2} + s$, with $0 \leq s \leq T$, define $f(a) = \binom{T}{3} + \binom{s}{2}$. Let G be a p -group of class two and prime exponent, with $\text{rank}(G/Z(G)) = n$ and $\text{rank}([G, G]) = m$. If

$$f\left(\binom{n}{2} - m + 1\right) < n,$$

then G is capable. (Received August 07, 2005)