1014-33-1156 James C. Griffin* (jgriffin@math.ucf.edu), Dept of Mathematics, University of Central Florida, Orlando, FL 32826. Orthogonal Polynomials Arising from Generalized Trigonometric Identities. Preliminary report.

The equation $P_n^2 - (x^2 - 1)Q_n^2 = 1$ where P_n and Q_n are polynomials of degree n and n-1 respectively, uniquely determines the P_n and Q_n for each n. The polynomials in this case correspond to the Chebyshev polynomials of 1st and 2nd kind. I will discuss the relationship between solutions to higher degree generalizations of this equation and other sequences of orthogonal polynomials. One such generalization is the equation $P_n^3 + (x^3 - 1)Q_n^3 + (x^3 - 1)^2R_n^3 - 3(x^3 - 1)P_nQ_nR_n = 1$ where R_n is of degree n - 2. (Received September 27, 2005)