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**Paul T Taylor\*** ([taylorp@math.mcmaster.ca](mailto:taylorp@math.mcmaster.ca)), Department of Mathematics and Statistics, McMaster University, 1280 Main St. W, Hamilton, Ontario L8S4K1, Canada. *Bochner-Riesz means With Respect to a Rough Distance Function.*

The generalized Bochner-Riesz operator  $S^{R,\lambda}$  may be defined as

$$S^{R,\lambda}f(x) = \mathcal{F}^{-1} \left[ \left(1 - \frac{\rho}{R}\right)_+^\lambda \widehat{f} \right] (x)$$

where  $\rho$  is an appropriate distance function and  $\mathcal{F}^{-1}$  is the Inverse Fourier Transform. The behavior of  $S^{R,\lambda}$  on  $L^p(\mathbf{R}^d \times \mathbf{R})$  is described for  $\rho(\xi', \xi_{d+1}) = \max\{|\xi'|, |\xi_{d+1}|\}$ , a rough distance function. We conjecture that this operator is bounded on  $\mathbf{R}^d \times \mathbf{R}$  when  $\lambda > \max\{d(\frac{1}{2} - \frac{1}{p}) - \frac{1}{2}, 0\}$  and  $p < 2 + \frac{6}{d-3}$ , and unbounded when  $p \geq 2 + \frac{6}{d-3}$ . This conjecture is verified for large ranges of  $p$ . (Received September 22, 2005)