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Consider a sequence  $\{X_k, k \geq 1\}$  of i.i.d. random variables with subexponential d.f.  $F$  ( $F \in \mathcal{S}$ ), that is

$$P\{X_1 + X_2 > x\} \sim 2P\{X_1 > x\} \text{ as } x \rightarrow \infty.$$

Using the convention  $X_0 = 0$ , we write

$$X_{(n)} = \max_{0 \leq k \leq n} X_k, \quad S_n = \sum_{k=0}^n X_k, \quad S_{(n)} = \max_{0 \leq k \leq n} S_k.$$

Using the Pollaczek-Spitzer identity, Sgibnev (1996) studied the asymptotic behavior of the tail probability of  $S_{(n)}$  in the case of i.i.d. summands. In particular, when  $F \in \mathcal{S}$ , he proved that  $P(S_{(n)} > x) \sim n\bar{F}(x)$ , where  $\bar{F}(x) = P\{X > x\}$ .

In the talk we drop the assumption of identically distributed random variables with  $F \in \mathcal{S}$  and assume instead that  $X_k, k \geq 1$  has a long-tailed distribution function  $F_k$  ( $F_k \in \mathcal{L}$ ), that is  $P\{X_k > x + a\} \sim P\{X_k > x\}$  as  $x \rightarrow \infty$ . In this more general setup we explore under which conditions the asymptotic equalities

$$P\{S_{(n)} > x\} \sim P\{X_{(n)} > x\} \sim P\{S_n > x\} \sim \sum_{k=1}^n \bar{F}_k(x).$$

are valid.

An extension to negatively associated subexponential random variables will be discussed as well. This generalizes a result of Wang and Tang (2004). (Received September 25, 2005)