

1014-76-470

Pangyen Weng* (pweng@ramapo.edu), Tamarack A, 505 Ramapo Valley Rd., Ramapo College of New Jersey, Mahwah, NJ 07430. *On Sobolev Spaces of Divergence-Free Vector Fields*. Preliminary report.

We consider the equivalence of two Sobolev spaces of divergence-free vector fields in open bounded domains. Define the following terms:

- Energy norm $\|\cdot\|$:

$$\|\mathbf{u}\| = \left\{ \sum_i \int_{\Omega} |\nabla u_i|^2 d\mathbf{x} \right\}^{1/2}.$$

- $\mathbf{D}(\Omega) = (\mathcal{C}_0^\infty(\Omega))^d$.
- $\mathcal{V} = \{\mathbf{u} \in \mathbf{D}(\Omega) : \operatorname{div} \mathbf{u} = 0\}$.
- $V(\Omega) =$ the closure of \mathcal{V} in $\|\cdot\|$.
- $\tilde{V}(\Omega) = \{\mathbf{u} \in \mathbf{W}_0 : \operatorname{div} \mathbf{u} = 0\}$, \mathbf{W}_0 is the closure of $\mathbf{D}(\Omega)$ in $\|\cdot\|$.

We prove that $V(\Omega) = \tilde{V}(\Omega)$ in \mathbb{R}^2 . We then generalize the results to open, bounded, and axisymmetric domains in \mathbb{R}^3 . The key to these results is a theorem on Sobolev spaces by Hedberg, the technique of stream functions, and the topological structure of \mathbb{R}^2 . (Received September 16, 2005)