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Given a semigroup  $(S, \cdot)$ , an interassociate of S is a semigroup with the same underlying set S and a binary operation \* such that  $a \cdot (b * c) = (a \cdot b) * c$  and  $a * (b \cdot c) = (a * b) \cdot c$ . We examine interassociativity for the free commutative semigroup on n generators, denoted  $(S, \cdot)$ . We begin by determining the structure of all interassociates of  $(S, \cdot)$ . It turns out that every interassociate can be written in the form  $(S, *_{\bar{k}})$ , depending only on a n-tuple  $\bar{k} = (k_1, \ldots, k_n)$ . Next, if  $(S, *_{\bar{k}})$  and  $(S, *_{\bar{\ell}})$  are isomorphic interassociates of  $(S, \cdot)$  such that  $\phi(x_i) = x_j$ , for  $x_i$  and  $x_j$  in the generating set of S, then  $k_i = \ell_j$ . Finally, we will see that  $(S, *_{\bar{k}})$  is isomorphic to  $(S, *_{\bar{\ell}})$  if and only if  $\{k_i\}_{i=1}^n$  is a permutation of  $\{\ell_i\}_{i=1}^n$ . (Received September 25, 2006)