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Lie's prolongation method calculates the infinitesimal symmetries of the wave equation on  $\mathbf{R}^{n+1}$  to be  $\mathfrak{g} = \mathfrak{so}(2, n + 1)$  plus an infinite dimensional piece and one obtains an action of  $\mathfrak{g}$  on the smooth solutions of the wave equation. However, this action does not exponentiate to an action of the group  $G = SO(2, n + 1)$ . To obtain an action of the group  $G$  (or a two-fold cover of  $G$  if  $n$  is even), we restrict the action to a natural subspace of functions that is defined by restricting sections of a certain line bundle on a compact homogenous space  $G/P$  to an open and dense copy of  $\mathbf{R}^{n+1}$ . The wave operator then arises from a combination of the Casimir elements of a distinguished copy of  $\mathfrak{sl}(2, \mathbf{R})$  and  $\mathfrak{so}(n)$ . We use this fact to study the resulting representations and to give explicit formulas for solutions of the wave equation. (Received September 25, 2006)