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For the positive integer  $n$ , let  $a_n$  count the number of compositions of  $n$  where the last summand is odd. Then  $a_n = (\frac{1}{3})(-1)^{n-1} + (\frac{2}{3})2^{n-1} = J_{n-1}$ , where  $J_n$  (for  $n \geq 0$ ) denotes the  $n$ -th Jacobsthal number. The results we determine for these compositions include the following, where  $n, k$  are positive integers: (1)  $a_{n,k}$ , the number of times the summand  $k$  appears among the  $a_n$  compositions of  $n$ ; (2)  $s_{n,k}$ , the number of these compositions of  $n$  where  $k$  is the first summand; (3) the number of plus signs and the number of summands that appear among the  $a_n$  compositions; (4) the number of runs that occur among the compositions; and (5) the numbers of levels, rises and descents that occur among the  $a_n$  compositions. In addition, comparable results for the palindromes found among the  $a_n$  compositions are examined. (Received September 14, 2006)