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Gareth E Roberts* (groberts@radius.holycross.edu), Dept. of Mathematics and CS,
College of the Holy Cross, 1 College Street, Worcester, MA 01610, and **Trevor M O'Brien**. *An
Amazing Bifurcation Diagram Arising from Newton's Method.*

Newton's method applied to a complex polynomial can fail quite miserably, even on a fairly large open set of initial guesses. We investigate Newton's method applied to the quartic family $p_\lambda(z) = (z + 1)(z - 1)(z - \lambda)(z - \bar{\lambda})$ where $\lambda \in \mathbb{C}$ is a parameter. The symmetric location of the roots allows for some easy reductions. Classifying those λ -values where the method fails on an open set leads to a complicated yet marvelous picture in the λ -parameter plane full of Mandelbrot-like sets, tricorns and swallowtails. (Received September 22, 2006)