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Bryan Clair* (bryan@slu.edu), Saint Louis University, Mathematics and Computer Science, 220 N. Grand Ave., St. Louis, MO 63103. *L^2 zeta functions and infinite cyclic covers of graphs.*

Suppose that finite graphs $X = X_0, X_1, X_2, \dots$ all cover X and converge to an infinite graph Y . Then the Ihara zeta functions of the X_i converge, suitably normalized, to a zeta function associated to Y called the L^2 zeta function. The L^2 zeta function satisfies a formula similar to the Ihara-Hashimoto rationality formula, but is not in general a rational function. In the case $Y \rightarrow X$ is an infinite cyclic covering, the L^2 zeta function is algebraic, has an associated Riemann surface with finitely many sheets, and satisfies functional equations analogous to those for the Ihara zeta function. (Received September 06, 2007)