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**Patrick Bahls\*** (pbahls@unca.edu), Department of Mathematics, University of North Carolina, Asheville, CPO #2350, Asheville, NC 28804-8511, and **Nicole A. Gin.** *Clawfreeness of powers of graphs.* Preliminary report.

The question of whether a graph  $G$  contains the *claw*  $K_{1,3}$  as an induced subgraph is an interesting one. For instance, a good deal is known about the hamiltonicity and more general cycle structure of claw-free graphs, and clawfreeness implies nice properties about certain graph polynomials. The *powers*  $G^n$  of a graph  $G$  play a similarly important role in many areas of graph theory.

For any  $n \in \mathbb{N}$  we determine a minimal collection  $\mathcal{G}_n$  of graphs such that  $|\mathcal{G}_n| = n$  and if the power  $G^n$  contains a claw then some  $H \in \mathcal{G}_n$  appears as an induced subgraph of  $G$ . We use this result to describe precisely those powers of a tree  $T$  which are claw-free and close with several open problems concerning more general graphs  $G$ . (Received July 06, 2011)