Let $\lambda(n)$ denote the Liouville function. Complementary to the prime number theorem, Chowla conjectured that

**Conjecture (Chowla).**

$$\sum_{n \leq x} \lambda(f(n)) = o(x)$$

for any polynomial $f(x)$ with integer coefficients, not in the form of $bg^2(x)$, where $b$ is a constant.

Chowla’s conjecture is proved for linear functions but for the degree greater than 1, the conjecture seems to be extremely hard and still remains wide open. One can consider a weaker form of Chowla’s conjecture, namely,

**Conjecture 1 (Cassaigne, et al).** If $f(x) \in \mathbb{Z}[x]$ and is not in the form of $bg^2(x)$ for some $g(x) \in \mathbb{Z}[x]$ and constant $b$, then $\lambda(f(n))$ changes signs infinitely often.

Although it is weaker, Conjecture 1 is still wide open for polynomials of degree $> 1$. In this talk, I will describe some recent progress made while studying Conjecture 1 for the quadratic polynomials. This is joint work with Peter Borwein and Stephen Choi. (Received July 28, 2011)