Let $G$ be a finite group. One can if there are any Galois extensions of $\mathbb{Q}$ ramified at 2 (and possibly at infinity) with Galois group $G$. Using a combination of computational and theoretical techniques, we show that the answer is no for a large number of $G$. (Received August 08, 2011)