An operator $T$ on a Hilbert space $H$ is called complex symmetric if there is an involutive, isometric, antilinear operator $C$ on $H$ such that $T = CT^*C$. This talk, based on ongoing work with Stephan Ramon Garcia, explores which composition operators on various weighted Hardy spaces can possess the property of complex symmetry. (Received September 22, 2011)