Global integration and approximation problems arise naturally in many applications of mathematics to planet Earth. In this talk we survey recent developments and challenges relevant to geomathematics, with an emphasis on polynomial and radial basis function methods. (Received September 20, 2011)