This talk will present a survey of recent work on pseudocodewords. After introducing and explaining their importance, I shall describe a variety of algebraic tools that have been used to study them. There are various notions of pseudoweight for pseudocodewords and I shall explain how the above tools have been used to make progress on some open problems concerning pseudoweight bounds. (Received September 18, 2011)