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**Asher M Kach, Karen Lange and Reed Solomon\*** ([david.solomon@uconn.edu](mailto:david.solomon@uconn.edu)),  
Department of Mathematics, University of Connecticut, U-3009, Storrs, CT 06269. *Turing degrees  
of orders on torsion-free abelian groups.*

The space of orders on a computable formally real field or computable torsion-free abelian group forms a  $\Pi_1^0$  class. In the case of fields, one can represent any  $\Pi_1^0$  class (up to Turing degree) by the space of orders in some computable field. However, this property fails for computable abelian groups even for  $\Pi_1^0$  classes which are classically homeomorphic to Cantor space. This talk will focus on a recent construction showing that for certain computable torsion-free abelian groups, one can always find a presentation for which the set of degrees of orderings is not upwards closed in the Turing degrees. (Received September 21, 2012)