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George M. Bergman* (gbergman@math.berkeley.edu), Department of Mathematics,
University of California, Berkeley, CA 94720-3840. *Families of ultrafilters, and homomorphisms on
infinite direct product algebras.*

In the preprint of which we will give some highlights, criteria are obtained for a filter \mathcal{F} of subsets of a set I to be an intersection of finitely many ultrafilters, respectively finitely many κ -complete ultrafilters for a given uncountable cardinal κ . Using these criteria, general results are deduced concerning homomorphisms on infinite direct product groups, yielding short proofs of some results in the literature: the Łoś-Eda theorem (on homomorphisms from a not-necessarily-countable direct product of modules to a slender module), and some results of N. Nahlus and the author on homomorphisms on direct products of not-necessarily-associative k -algebras. The same tools allow some related results to be strengthened, and yield an analog to one of these with nonabelian groups in place of k -algebras.

We briefly examine to what other structures the one might apply the methods that work, as noted above, for k -algebras on the one hand and for nonabelian groups on the other.

In a final section, the Erdős-Kaplansky Theorem on dimensions of vector spaces D^I (D a division ring) is extended to reduced products D^I/\mathcal{F} .

For the preprint, see http://math.berkeley.edu/~gbergman/papers/cap_ultra.pdf (Received September 25, 2012)