We study toggle group actions and cyclic sieving phenomena on generalized order ideals of posets; these correspond to Schröder paths in a special case. We also examine generalizations of alternating sign matrices arising from this construction and explore algebraic and geometric connections. This is a sequel to our paper, “Promotion and rowmotion.” (Received September 25, 2012)