

1086-11-2323

Alexander Berkovich* (alex@ufl.edu). *On Certain Partition Inequalities.*

It is a well known corollary of the celebrated Rogers-Ramanujan identities that the coefficients in q -series expansion of the difference of two infinite products

$$1/(q, q^4;^5)_{inf} - 1/(q^2, q^3; q^5)_{inf}$$

are all non-negative.

Surprisingly, it is also true for the finite products

$$1/(q, q^4;^5)_L - 1/(q^2, q^3; q^5)_L, \quad L \text{ is integer } > 0.$$

In my talk I will discuss a simple injective argument due to Frank Garvan and myself that proves it.

Next, I review a new theorem by George Andrews: The q -series expansion of

$$1/(q, q^5, q^6;^5)_L - 1/(q^2, q^3, q^7; q^8)_L, \quad L \text{ is integer } > 0$$

has non-negative coefficients.

Finally, I discuss a recent generalization of this theorem by Keith Grizzell and myself :

For any $L > 0$ and any odd $y > 1$, the q -series expansion of

$$1/(q, q^{y+2}, q^{2y}; q^{2y+2})_L - 1/(q^2, q^y, q^{2y+1}; q^{2y+2})_L$$

has non-negative coefficients. (Received September 25, 2012)