

1086-20-2001

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Room 203, 2360 S. Gaylord St, Denver, CO 80208. *Loops categorically isomorphic to Bruck loops.*

Given a uniquely 2-divisible group, we give a construction (originally used by Baer) for creating a new class of loops we call  $\Gamma$ -loops. Our main goal is showing a categorical isomorphism between uniquely 2-divisible Bruck loops and uniquely 2-divisible  $\Gamma$ -loops. Once this has been established, we can use the well known structure of Bruck loops of odd order to derive the Lagrange, Cauchy, Odd Order, Sylow and Hall theorems for  $\Gamma$ -loops of odd order, as well as the nilpotence of finite  $\Gamma$ - $p$ -loops ( $p$  odd). In particular, this answers an open problem regarding the existence of Sylow  $p$ -subloops and Hall  $\pi$ -subloops in commutative automorphic loops. (Received September 24, 2012)