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We'am M. Jasim* (s_weam@yahoo.com), Texas A & M International University, Department of Engineering, Mathematics, and, Physics LBV 312 5201 University Blvd, Laredo, TX 78041, and **robert r. kallman** (kallman@unt.edu), University of North Texas, Department of, Mathematics GAB 435, 1155 Union Circle #311430, Denton, TX 76203-5017. *Algebraically Determined Semidirect Products.*

Let G be a Polish (i.e., complete separable metric topological) group. Define G to be an algebraically determined Polish group if given any Polish group L and an algebraic isomorphism $\varphi : L \rightarrow G$, then φ is a topological isomorphism. The purpose of this paper is to prove a general theorem that gives useful sufficient conditions for a semidirect product of two Polish groups to be algebraically determined. This general theorem will provide a flowchart or recipe for proving that some special semidirect products are algebraically determined. For example, it may be used to prove that the natural semidirect product of H and G , where H is the additive group of a separable Hilbert space and G is a Polish group of unitaries on H acting transitively on the unit sphere with $-I \in G$, is algebraically determined. An example of such a G is the unitary group of a separable irreducible C^* -algebra with identity on H . Not all nontrivial semidirect products of Polish groups are algebraically determined, for it is known that the Heisenberg group is not an algebraically determined Polish group. (Received June 26, 2012)