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Multi-indexed orthogonal polynomials satisfy second order differential (difference) equations. They start at degree  $\ell \geq 1$  and form a complete set of orthogonal functions. They are obtained by deforming the classical orthogonal polynomials (e.g. Jacobi, q-Racah, Askey-Wilson etc) in terms of multiple Darboux-Crum transformations and their difference analogues [1,2,3]. In the case of Jacobi, they form global solutions of Fuchsian differential equations having  $3 + \ell$  regular singularities [1]. Multi-indexed q-Racah and Racah polynomials and their reductions provide ample examples of exactly solvable birth and death processes [4].

[1] S. Odake and R. Sasaki, “Exactly solvable quantum mechanics and infinite families of multi-indexed orthogonal polynomials,” *Phys. Lett. B* **702** (2011) 164-170, [arXiv:1105.0508\[math-ph\]](https://arxiv.org/abs/1105.0508).

[2] S. Odake and R. Sasaki, “Multi-indexed (q-)racah polynomials, *J. Phys. A* **45** (2012) in press, [arXiv:1203.5868\[math-ph\]](https://arxiv.org/abs/1203.5868).

[3] S. Odake and R. Sasaki, “Multi-indexed Wilson and Askey-Wilson Polynomials,” [arXiv:1207.5584\[math-ph\]](https://arxiv.org/abs/1207.5584).

[4] R. Sasaki, “Exactly Solvable Birth and Death Processes,” *J. Math. Phys.* **50** (2009) 103509 (18 pp), [arXiv:0903.3097\[math-ph\]](https://arxiv.org/abs/0903.3097). (Received August 29, 2012)