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Differential Harnack Estimates for Fisher's Equation.

In this talk we derive two differential Harnack estimates for positive solutions of the second order partial differential equation $f_t = \Delta f + cf(1 - f)$, known as Fisher's Equation. This equation is useful as a fundamental model for reaction-diffusion equations across many fields.

If we let (M^n, g) be an n -dimensional compact Riemannian manifold with non-negative Ricci curvature and $f : M \times [0, \infty) \rightarrow \mathbb{R}$ be a positive solution to Fisher's Equation, then we derive a Harnack inequality of the form $\Delta(\log f) + \alpha|\nabla(\log f)|^2 + \beta f + \phi(t) \geq 0$, with an explicit $\phi(t)$ and bounds on α and β . By loosening the restrictions on M to complete but non-compact, we then derive a second inequality of the same general form but with a more intricate function $\phi(t)$. (Received September 25, 2012)