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Travis Wolf* (travs-wolf@uiowa.edu), Travis Wolf, Department of Mathematics, 14 MacLean Hall, Iowa City, IA 52242-1419. *Coisometric Extensions of Completely Contractive Covariant Representations*. Preliminary report.

A C^* -correspondence E over a C^* -algebra A is a sort of generalized Hilbert space, together with a homomorphism $\phi : A \rightarrow \mathcal{L}(E)$ giving a left action of A on E , where $\mathcal{L}(E)$ denotes the C^* -algebra of bounded adjointable operators on E . A *generalized transfer operator* for ϕ is a completely positive linear map $\tau : \mathcal{L}(E) \rightarrow A$ with the property that $\tau(\phi(a)X) = a\tau(X)$ for $a \in A$ and $X \in \mathcal{L}(E)$. Assuming ϕ has a generalized transfer operator, we give a way of constructing a unique coisometric extension for any so-called *completely contractive covariant representation* of (E, A) . Completely contractive covariant representations are generalizations of contractive operators to the setting of C^* -correspondences, and in the course of the construction we will examine several examples. Notable among them is the special case where $E = \mathbb{C}^d$ and $A = \mathbb{C}$, in which case a (unital) generalized transfer operator is simply a state on $M_d(\mathbb{C})$.

Our analysis extends work of Muhly and Solel and complements studies by Ball and Vinnikov, Bratteli and Jorgensen, Exel, and Popescu. (Received September 23, 2012)