Hales proved that regular hexagons provide the least-perimeter way to partition the plane into unit areas. What are the best tilings by pentagons? Could it possibly help to mix in some non-convex pentagons? (Received September 25, 2012)