

1086-92-1641

Tilahun A Muche* (muchet@savannahstate.edu), Savannah State University, Engineering Technology and Mathematics Dept., 3219 College Street, Savannah, GA, 31404, Savannah, GA 31404. *Hamiltonian sets of polygonal paths in a 4-valent spatial graphs*. Preliminary report.

Graphs with 4 valent rigid vertices and two end points are called simple assembly graphs. The *assembly number* of Γ , denoted by $An(\Gamma)$, is defined by $An(\Gamma) = \min\{k \mid \text{there exists a Hamiltonian set of polygonal paths } \{\gamma_1, \dots, \gamma_k\} \text{ in } \Gamma\}$ where polygonal paths are paths that take “90° turn” at each vertex. For a positive integer n , we define *minimal realization number for n* to be $R_{min}(n) = \min\{|\Gamma| : An(\Gamma) = n\}$, where $|\Gamma|$ is the number of 4-valent vertices in Γ . For a positive integer n , a graph Γ such that $R_{min}(n) = |\Gamma|$ is called minimal realization graph. We denote by $\mathcal{R}_{min}(n)$, the set of minimal realization graphs for some positive integer n . Each $\Gamma \in \mathcal{R}_{min}(n)$ has the property that $|\Gamma| \leq 3n - 2$ and $R_{min}(n) < R_{min}(n + 1)$ for every natural number n . The assembly graph $\hat{\Gamma}^0$ obtained from a given assembly graph Γ by substituting every edge with a loop, is called *loop-saturated graph*. We prove that loop saturated assembly graphs achieve the bound of $3n - 2$ and if a simple assembly graph Γ with $An(\Gamma) = k$ has no loops then it is not in $\mathcal{R}_{min}(k)$. (Received September 23, 2012)