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**Enrique Treviño\***, 555 N. Sheridan, Lake Forest College, Department of Mathematics, Lake Forest, IL 60045, and **Paul P Pollack**. *The primes that Euclid forgot*.

Let  $q_0 = 1$ . Supposing that we have defined  $q_j$  for all  $0 \leq j \leq k$ , let  $q_{k+1}$  be a prime factor of  $1 + \prod_{j=1}^k q_j$ . As was shown by Euclid over two thousand years ago,  $q_1, q_2, q_3, \dots$  is then an infinite sequence of distinct primes. The sequence  $\{q_i\}$  is not unique, since there is flexibility in the choice of the prime  $q_{k+1}$  dividing  $1 + \prod_{j=1}^k q_j$ . Mullin suggested studying the two sequences formed by (1) always taking  $q_{k+1}$  as small as possible, and (2) always taking  $q_{k+1}$  as large as possible. For each of these sequences, he asked whether every prime eventually appears. Recently, Booker showed that the second sequence omits infinitely many primes. We give a completely elementary proof of Booker's result. (Received September 17, 2013)