The study of composed inclusions of two subfactors was initiated by D. Bisch and U. Haagerup. We will discuss the classification in the case that the principal graphs of the two subfactors are $A_3$ and $A_4$. We answer a question posed by D. Bisch and U. Haagerup in 1994. (Received August 24, 2013)