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Let  $E$  be a real vector space equipped with an inner product  $x \cdot y$  and the corresponding norm  $\|x\|$ . We assume that  $E$  is non trivial  $\dim E \geq 1$ , and  $T : E \rightarrow E$  is a linear transformation. As usual  $T$  is *isometric* if  $\|Tx\| = \|x\|$  for all  $x \in E$ ;  $T$  is a *similarity* if it is isometric up-to a positive constant. It is well known that  $T$  is a similarity if and only if it preserves orthogonality, i.e.  $x \cdot y = 0$  implies  $Tx \cdot Ty = 0$  for all  $x, y \in E$ . A similarity preserves any angle which means that for all  $x, y \in E$  the equality  $\|x\| \|y\|(Tx \cdot Ty) = \|Tx\| \|Ty\|(x \cdot y)$  holds. In this paper we prove that in an inner product space, linear transformations preserving angles with a given single magnitude  $0 < \alpha < \pi$ , are similarities. In other words, for a linear transformation  $T$  to be a similarity it is sufficient that there exists an  $0 < \alpha < \pi$  such that for all  $x, y \in E$ , the equality  $x \cdot y = \|x\|\|y\| \cos \alpha$  implies  $Tx \cdot Ty = \|Tx\|\|Ty\| \cos \alpha$ . (Received September 09, 2013)