We consider two natural classes of minimal laminations in three-manifolds. Both classes may be thought of as limits – in different senses – of embedded minimal disks. In both cases, we prove that, under a natural geometric assumption on the three manifold, the leaves of these laminations are topologically either disks, annuli or Möbius bands. This answers a question posed by Hoffman and White. (Received September 08, 2013)