In this talk, we present a model of Hele-Shaw flow in which two immiscible fluids react and produce a gel-like phase at the interface. Since the gel-phase can make the interface stiff, we model the interface as an elastic membrane whose bending stiffness depends on the local curvature. We show linear stability analysis and preliminary numerical results on fingering instability in such a system. (Received September 09, 2013)