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Let G be a Polish group. G is algebraically determined Polish group if given any Polish group L and an algebraic isomorphism $f : L \rightarrow G$, then f is a topological isomorphism. Let $M(n;R) = R^{(n)^2}$ be all $n \times n$ matrices with coefficients in R , and let the group G in the above definition be the natural semidirect product $R^n \times G(n)$, where $n \geq 2$ and $G(n)$ is one of the following groups: either the general linear group $GL(n;R) = \{A \in M(n;R) \mid \det(A) \neq 0\}$, or the special linear group $SL(n;R) = \{A \in GL(n;R) \mid \det(A) = 1\}$, or $|SL(n;R)| = \{A \in GL(n;R) \mid |\det(A)| = 1\}$, or $GL^+(n;R) = \{A \in GL(n;R) \mid \det(A) > 0\}$. We will prove that the natural semidirect product $R^n \times G(n)$ is an algebraically determined Polish group. In addition, a key intermediate result that requires a fair amount of labor is to prove that $f^{-1}(SO(n;R))$ is an analytic subgroup of L , where $SO(n;R)$ is the $n \times n$ rotation group with determinant one and $SO(n;R) \subset SL(n;R) \subset GL(n;R)$ for every $n \geq 2$. The proofs are somewhat delicate, for there are nontrivial natural semidirect products that are not algebraically determined. For example, the natural semidirect product $R^3 \times SO(3;R)$ surprisingly has a discontinuous automorphism. Also, $GL(n;R)$ is not algebraically determined Polish group. (Received September 13, 2013)