

1096-VM-362

Timothy C Melvin* (tmelvin@carroll.edu), Tim Melvin, 1601 N Benton Ave, Mathematics Department, Helena, MT 59625. *Spectrally Arbitrary Patterns and Algebraic Solutions.*

We say that an $n \times n$ zero-nonzero matrix pattern \mathbb{A} is spectrally arbitrary over the field \mathbb{F} if for every monic, n -degree polynomial $p(t)$ with coefficients from \mathbb{F} , there exists a matrix A over \mathbb{F} with zero-nonzero pattern \mathbb{A} such that the characteristic polynomial of A is $p(t)$. We will use Hilbert's Nullstellensatz to show that if a pattern is spectrally arbitrary over \mathbb{C} , then it is also spectrally arbitrary over $\overline{\mathbb{Q}}$, the algebraic closure of \mathbb{Q} . More generally, this result shows that if any system of multivariate polynomials with algebraic coefficients has a common zero, then there will be a common zero whose components are all algebraic. (Received August 30, 2013)