

1096-VN-1216

**Ralph P. Grimaldi\*** ([grimaldi@rose-hulman.edu](mailto:grimaldi@rose-hulman.edu)), Mathematics Department, RHIT, 5500 Wabash Avenue, Terre Haute, IN 47803. *Odd-Neighbored Subsets.*

For  $n \geq 1$ , a subset  $S$  of  $[n] = \{1, 2, 3, \dots, n\}$  is called *odd-neighbored* if for each even integer  $k \in S$ ,  $k - 1 \in S$ , and if  $k + 1 \leq n$ , then  $k + 1 \in S$ . When  $n = 4$ , for example, we find eight such subsets - namely,  $\emptyset$ ,  $\{1\}$ ,  $\{3\}$ ,  $\{1, 3\}$ ,  $\{1, 2, 3\}$ ,  $\{3, 4\}$ ,  $\{1, 3, 4\}$ , and  $\{1, 2, 3, 4\}$ . In general, there are  $F_{n+2}$  odd-neighbored subsets of  $[n]$ , where  $F_n$  denotes the  $n$ th Fibonacci number.

Formulas for the following are derived for these types of subsets: 1) the total number of elements that appear, as well as the numbers of odd and even elements; 2) the sum of all the elements that appear, as well as the sums for the odd and even elements; and, 3) the number of strings of consecutive integers in these odd-neighbored subsets. (Received September 13, 2013)