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John S. Caughman, Charles L. Dunn, Joshua D. Laison* (jlaison@willamette.edu),
Nancy Ann Neudauer and Colin L. Starr. *Minimum Representations of Rectangle Visibility Graphs.* Preliminary report.

Let S be a set of nonintersecting open rectangles in the plane with horizontal and vertical sides. Two rectangles R_1 and R_2 are *visible* if there exists a *line of sight* between them, a horizontal or vertical line segment that intersects both R_1 and R_2 but no other object in S . We construct a graph G with a vertex for each rectangle in S , and an edge between two vertices if and only if their corresponding rectangles are visible. For a given graph G , if such a representation of G with rectangles exists then G is a *rectangle visibility graph (RVG)* and S is a *rectangle visibility representation* of G . Suppose the corners of the rectangles in S have integer coordinates. For a given RVG G , we ask how small its rectangle visibility representation can be. We think of the size of a rectangle visibility representation as the area of the smallest axis-parallel rectangle that encloses it (the *area* of S), or as the length of the shorter side of this rectangle (the *height* of S). We find the height of a rectangle visibility representation of a tree. We also ask for the RVG with n vertices and largest area. We begin answering this question for small values of n . (Received September 16, 2014)