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Mary Allison and **Bryan L Shader*** (bshader@uwyo.edu), 1000 E. University Ave, Math Department 3036, University of Wyoming, Laramie, WY 82071. *The minimum Kemeny constant problem.*

Let G is a connected graph on vertices, $1, 2, \dots, n$. We study a new optimization problem over the family $\text{Mark}(G)$ of all $n \times n$, symmetric, stochastic matrices $A = [a_{ij}]$, where the graph of A is an edge subgraph of G . More precisely, $a_{ij} \neq 0$ only if $i = j$, or $i \neq j$ and i is adjacent to j in G .

Boyd, Diaconis and Xiao in 2003 initiated the study of the Fastest Mixing Markov Chain on G , which corresponds to asking for the $A \in \text{Mark}(G)$ whose second largest eigenvalue modulus (SLEM) is smallest. It is known that the SLEM of A governs the rate of convergence of the corresponding Markov chain C .

The Kemeny constant, $K(A)$, of A is the expected number of steps for the chain C to start at a randomly selected state and first enter another randomly selected state. It provides some rough information about the short-term behavior of the Markov chain. If the graph of A is disconnected, then Kemeny constant is taken to be ∞ .

In this talk we study the problem of determining the inf of $K(A)$ over all $A \in \text{Mark}(G)$. General results about properties of optimizing matrices are proven, and the inf is determined for several families of graphs. (Received September 16, 2014)