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Given an  $n$ -cycle  $C$  in the symmetric group  $S_n$ , we say that a pair  $\langle i, j \rangle$  matches the  $\mu$  pattern if  $i < j$  and, as we traverse around  $C$  in a clockwise direction starting at  $i$  and ending at  $j$ , we never encounter a  $k$  with  $i < k < j$ . We say that a  $\mu$ -match  $\langle i, j \rangle$  in  $C$  is trivial if  $j = i + 1$  and is non-trivial otherwise. We say that an  $n$ -cycle  $C$  in  $S_n$  is incontractible if there is no  $i$  which is immediately followed by  $i + 1$  as we traverse in a clockwise direction around  $C$ . We show that the generating function  $NTI_{n,\mu}(q)$  of  $q$  raised to the number of nontrivial  $\mu$ -matches in  $C$  over all incontractible  $n$ -cycles  $C$  in  $S_n$  is a new  $q$ -analogue of the derangement numbers. We also show that there is a surprising connection between the charge statistic of Lascoux and Schützenberger and the polynomials  $NTI_{n,\mu}(q)$  in that the coefficient of the smallest power of  $q$  in  $NTI_{2k+1,\mu}(q)$  is the number of permutations in  $S_{2k+1}$  whose charge path is a Dyck path. (Received September 08, 2014)