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Wolfgang A. Schmid* (schmid@math.univ-paris13.fr). *When is the sum of two sets of lengths a set of lengths?*

Let H be a (commutative) atomic monoid, that is a commutative cancellative semi-group where each element can be written as a product of irreducible elements. For a non-invertible element $b \in H$ we say that n is a length of b if there exist irreducibles a_1, \dots, a_n such that $b = a_1 \dots a_n$. We denote by $L(b)$ the set of all n such that n is a length of b ; for an invertible element b we set $L(b) = \{0\}$.

The question to be discussed in this talk is under which conditions (on H) the set $L(b) + L(b') = \{n + n' : n \in L(b), n' \in L(b')\}$, for $b, b' \in H$, is guaranteed to be again a set of lengths, that is $L(b) + L(b') = L(c)$ for some $c \in H$. Note that $L(b) + L(b') \subset L(bb')$ but the inclusion can be strict.

In particular, we give a complete answer for the case of Krull monoids where each class contains a prime divisors.

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