

1106-11-1748

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In 1944, Dyson called for *direct* proofs of Ramanujan's congruences for  $p(n)$  that give concrete demonstrations of how the associated partitions can be systematically divided into equinumerous classes. He conjectured that a very simple statistic on partitions, called the "rank" of a partition, performs this division when considered modulo 5 and 7. In the same paper, Dyson hypothesized the existence of a different statistic, called the "crank," that would witness Ramanujan's congruence modulo 11 in the same way.

Recent results show that Dyson's ideas can be applied to partitions of  $n$  into exactly  $d$  parts, denoted by  $P(n, d)$ . Moreover, some of these new cranks for  $P(n, d)$  have a very surprising quality that is not shared with those for  $p(n)$ ; there are cranks for  $P(n, d)$  that witness *each and every* instance of divisibility modulo a given prime. We call these cranks *supercranks*.

In this talk, we make use of Ehrhart Geometry and other techniques to prove the following result:

**Theorem** (Breuer, Eichhorn, Kronholm). *Largest part minus smallest part is a supercrank for  $P(n, 3) \pmod{m}$  where  $m$  is any prime of the form  $6j - 1$ .* (Received September 15, 2014)