

1106-11-2441

**Kevin M Mugo\*** ([kevin.mugo@gmail.com](mailto:kevin.mugo@gmail.com)), W.Lafayette, IN 47906. *Mod 4 Galois Representations From Elliptic Curves and a Certain Brauer-Type Embedding Problem.*

Let  $\bar{\rho}_{E,4}$  be a surjective Galois representation, induced by the action of  $G_K$  on the 4-torsion points of an elliptic curve  $E$ , with invariant  $j_0$ . We show that the unique  $S_4$  field extension contained in  $K(E[4])$  is the splitting field of the principal quartic  $q(r) = r^4 + \frac{32}{j_0}r^2 + \frac{4}{j_0}$ . We show that  $L/K$  is a principal, quartic extension precisely when a certain Brauer-Severi variety has a  $K$ -rational point. When  $L/K$  is principal, and  $M/K$  is its normal closure, we show that the solvability of the embedding problem  $2S_4^+ \rightarrow \text{Gal}(M/K)$  is completely determined by the discriminant  $d_{L/K}$ . Moreover, we will show that if  $L/K$  is principal and the Hilbert symbol  $(-2, -d_{L/K})$  is trivial, then the embedding problem  $2S_4^+ \rightarrow \text{Gal}(M/K)$  is solvable. (Received September 16, 2014)