David Mehrle* (dmehrle@cmu.edu), Tomer Reiter (treiter@andrew.cmu.edu), Joseph Stahl (josephmichaelstahl@gmail.com), Dylan Yott (dtyott@gmail.com) and Steven Miller (sjm1@williams.edu). A Family of Rank 6 Elliptic Curves over Number Fields.

We construct a family of elliptic curves over a number field K, and prove that when K/\mathbb{Q} is Galois, each curve has rank six. Unlike most constructions, which only bound the rank, we find the rank exactly. By evaluating Legendre sums, we determine equations for curves \mathcal{E} with $A_{\mathfrak{p}}(\mathcal{E}) = -6$. Applying a theorem of Rosen and Silverman, we show that the rank is $-A_{\mathfrak{p}}(\mathcal{E})$. We obtain in this manner not only infinitely many elliptic curves over K, but also infinitely many elliptic surfaces, i.e., elliptic curves over the function field K(T). Additionally, we hypothesize that curves defined analogously over non-Galois extensions L/\mathbb{Q} also have rank six, which we prove in several cases, and determine bounds for all other cases. Moreover, we prove that when $K = \mathbb{Q}$, if there are any points of finite order in $\mathcal{E}(\mathbb{Q})$, they must have order three. However, we are able to modify our construction to find a family of curves with group $\mathcal{E}(\mathbb{Q}) = \mathbb{Z}^2 \oplus \mathbb{Z}/2\mathbb{Z}$. This generalizes work of Arms, Lozano-Robledo, and Miller, which only dealt with families over \mathbb{Q} . (Received August 27, 2014)