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The set $\{1, 25, 49\}$ is a 3-term collection of integers which forms an arithmetic progression; the common difference is 24. Hence the set $\{(1, 1), (5, 25), (7, 49)\}$ is a 3-term collection of rational points on the parabola $y = x^2$ whose y -coordinates form an arithmetic progression. Similarly, the set $\{6, 12, 18\}$ is a 3-term collection of integers which also forms an arithmetic progression; the common difference is 6. Hence the set $\{(6, 3), (12, 39), (18, 75)\}$ is a 3-term collection of rational points on the elliptic curve $y^2 = x^3 - 207$ whose x -coordinates form an arithmetic progression. Are there other examples such as these? What is the longest progression of rational points on either a quadratic or cubic curve such that either the x - or y -coordinates form an arithmetic progression? In this talk, we give a survey on what's known about arithmetic progressions on algebraic curves. We introduce elliptic curves as a means to show the non-existence of certain arithmetic progressions. We also introduce bielliptic curves in order to settle conjectures of Saraju P. Mohanty. (Received August 28, 2014)